

SUN2024 abstracts

SUN2024: SU(N) physics in quantum many-body systems:
theory, experiment, and numerics

We will gather together theorists, experimentalists, and experts on numerical methods in the field of SU(N) physics.

8-12 Jul 2024 Sendai (Japan)

Version: 2.0

Release: 20240524



Organizers:

Masahiko G. Yamada (Tokyo)

Yoshinori Imai (Tohoku)

Ji-Yao Chen (Sun Yat-sen University)

Miguel A. Cazalilla (DIPC)

Contents

| | |
|---|----|
| Invited talks | 4 |
| MASSIMO CAPONE: NOVEL MOTT STATES AND ENHANCED RESPONSES IN SYSTEMS WITH CONTROLLED BROKEN $SU(N)$ SYMMETRY | 4 |
| SIMON FÖLLING: TBA..... | 5 |
| KADEN R. A. HAZZARD: WHAT CAN THE $SU(N)$ HUBBARD MODEL TEACH US ABOUT CORRELATED MATTER?..... | 6 |
| LOIČ HERVIU: iDMRG SIMULATIONS OF THE $SU(N)$ J_1 - J_2 SPIN CHAINS | 7 |
| HUI-KE JIN: DENSITY MATRIX RENORMALIZATION GROUP BOOSTED BY GUTZWILLER PROJECTED WAVE FUNCTIONS AND ITS APPLICATIONS TO $SU(4)$ QUANTUM MAGNETISM..... | 8 |
| MATTHIEU MAMBRINI: $SU(N)$ SYMMETRIC PROJECTED ENTANGLED PAIR STATES : CONSTRUCTION AND APPLICATIONS..... | 9 |
| PIERRE NATAF: NUMERICAL METHODS TO INVESTIGATE $SU(N)$ FERMI-HUBBARD MODELS | 10 |
| RUI SAKANO: THEORY AND EXPERIMENT ON CURRENT NOISE OF $SU(N)$ ANDERSON IMPURITY | 11 |
| RICHARD T. SCALETTAR: QUANTUM SIMULATION STUDIES OF THE $SU(3)$ FERMI-HUBBARD MODEL | 13 |
| FLORIAN SCHRECK: TOWARDS ENCODING A QUDIT IN THE NUCLEAR SPIN OF ^{87}Sr | 14 |
| OWEN SHEEKEY: INTER-VALLEY COHERENCE, INTRINSIC AND EXTRINSIC SPIN-ORBIT COUPLING IN RHOMBOHEDRAL GRAPHENE | 15 |
| YOSUKE TAKASU: QUANTUM SIMULATION USING ULTRACOLD YB ATOMS WITH $SU(N)$ SYMMETRY | 16 |
| ANDREAS WEICHELBAUM: QSPACE: AN OPEN-SOURCE TENSOR LIBRARY FOR ABELIAN AND NON-ABELIAN SYMMETRIES | 17 |

| | |
|---|-----------|
| Oral presentations..... | 18 |
| LUIGI AMICO: FRACTIONAL QUANTIZATION OF $SU(N)$ MATTER-WAVE PERSISTENT CURRENTS. | 18 |
| WAYNE JORDAN CHETCUTI: PROBE FOR BOUND STATES OF $SU(3)$ FERMIONS AND COLOUR DECONFINEMENT | 19 |
| JUAN POLO GOMEZ: FLOW OF AN $SU(N)$ FERMIONIC MATTER-WAVE THROUGH A LOCALIZED BARRIER | 20 |
| CHEN-HOW HUANG: SYMMETRY BREAKING PATTERNS IN ITINERANT $SU(N)$ FERROMAGNETISM | 21 |
| AKIHISA KOGA: FERROMAGNETIC INSTABILITY FOR THE $SU(N)$ HUBBARD MODEL | 22 |
| RICO POHLE: DYNAMICS OF $SU(3)$ SPIN COHERENT STATES: SEMICLASSICAL METHOD AND ITS APPLICATION TO SPIN NEMATICS AND SPIN LIQUIDS IN SPIN-1 MAGNETS | 23 |
| Poster presentations | 24 |
| KAIJI MOTOYAMA: THREE-BODY FERMI-LIQUID EFFECTS ON TRANSPORT THROUGH THE $U = \infty$ $SU(N)$ ANDERSON IMPURITY | 24 |
| JORDI PERA: INTERACTION EFFECTS ON THE ITINERANT FERROMAGNETISM PHASE TRANSITION | 25 |
| NICOLAS SADOUNE: INTERPRETABLE PHASE CLASSIFICATION ON TRAPPED ION EXPERIMENT DATA BY TENSORIAL-KERNEL SVM | 26 |

Novel Mott states and enhanced responses in systems with controlled broken $SU(N)$ symmetry

Massimo Capone^{*1,2}

¹Scuola Internazionale Superiore di Studi Avanzati / International School for Advanced Studies – Italy

²IOM CNR, Via Bonomea 265, 34136 Trieste – Italy

Abstract

A large repulsion between quantum particles on a lattice can lead to their localization, as it happens for the electrons in Mott insulating materials. When we consider fermions with $N > 2$ flavours and the global $SU(N)$ is broken, even slightly, we can have novel quantum states that we can label as flavour-selective Mott states. We discuss the path from the theoretical prediction to the experimental detection of these states, with a particular emphasis on the results of a quantum simulation with Yb atoms where flavour-selective localization has been realized experimentally in a three-component system in the presence of a Raman coupling between two components (1). We briefly discuss the relation with solid-state counterparts (2).

We finally address how the combined presence of large Hubbard-like repulsion and Raman processes can lead to an enhancement of chiral currents close to the Mott transition (3) in one- or two-dimensional geometries.

This work reports about different manuscripts written with my coworkers including L. Del Re, M. Ferraretto, A. Richaud and L. de' Medici and with the group of L. Fallani in Florence, who performed the cold-atom experiments. The work is supported by MUR via PRIN 2020 (Prot. 2020JLZ52N 002) programs, PRIN 2022 (Prot. 20228YCY7), MUR Project No. PE0000023-NQSTI and ICSC–Centro Nazionale di Ricerca in High Performance Computing, Big Data and Quantum Computing, funded by European Union – NextGenerationEU (Grant number CN00000013)

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*Speaker

TBA

Simon Fölling*^{†1,2}

¹Ludwig Maximilians-Universität München (LMU) – Schellingstr. 4, 80799 München, Germany

²Max-Planck-Institut für Quantenoptik (MPQ) – Hans-Kopfermann-Str. 1 85748 Garching, Germany

Abstract

TBA

*Speaker

[†]Corresponding author: simon.foelling@lmu.de

What can the $SU(N)$ Hubbard model teach us about correlated matter?

Kaden Hazzard*¹

¹Rice University – United States

Abstract

The interplay of recent ultracold alkaline-earth atom experiments in optical lattices and theoretical calculations of the $SU(N)$ Hubbard model describing them is opening a new window into strongly correlated matter. I will argue that these $SU(N)$ systems have unique, important attributes that are absent in conventional $SU(2)$ cold atom experiments. One such attribute is that some $SU(N)$ experiments are now firmly out of the regime reachable with controlled numerical calculations, which makes the experiments powerful quantum simulators.

I will first discuss the current state of theoretical calculations in understanding the experiments, and then suggest avenues for algorithm development guided by these powerful quantum simulations.

I will also show how conceptual questions, such as the nature of holes doped into antiferromagnets, are ripe to be probed in these systems. As a concrete example, I will discuss the intriguing picture of the one-hole doped $SU(3)$ Hubbard model presented by geometric string theory and its corroboration in DMRG calculations. I will present how this emerging can be studied in the first generation of alkaline-earth atom quantum gas microscope now coming online.

*Speaker

iDMRG simulations of the $SU(N)$ J1-J2 spin chains

Loic Herviou^{*†1}, Sylvain Capponi², and Philippe Lecheminant³

¹Univ. Grenoble-Alpes, CNRS, LPMMC, 38000 Grenoble, France – Centre national de la recherche scientifique - CNRS (France), LPMMC Grenoble – France

²Laboratoire de Physique Théorique, Université de Toulouse, CNRS, UPS, France – Laboratoire de Physique Théorique, Université de Toulouse, CNRS, UPS, France – France

³Laboratoire de Physique Théorique et Modélisation, CNRS, CY Cergy Paris Université, 95302 Cergy-Pontoise Cedex, France – Laboratoire de Physique Théorique et Modélisation, CNRS, CY Cergy Paris Université, 95302 Cergy-Pontoise Cedex, France – France

Abstract

According to field theory computations, the zero-temperature phase diagram of the J1-J2 $SU(N)$ spin chains depends on the parity of N . While a transition from critical to a gapped $SU(N)$ valence bond solid is always observed at small J_2 s, we find that for odd N a gapless phase reopens in the large J_2 limit. This phase is in the $SU(N)_1$ universality class due to the existence of a massless renormalization group flow from $SU(N)_2$ to $SU(N)_1$ conformal field theories.

In this talk, after presenting our RG analysis, I will discuss the strengths and limits of (i)DMRG applied to $SU(N)$ spin chains, which allowed us to confirm (some of) the field theory predictions, and also revealed the existence of a commensurate to incommensurate transition within the valence bond phase for even N .

*Speaker

†Corresponding author: loic.herviou@gmail.com

Density matrix renormalization group boosted by Gutzwiller projected wave functions and its applications to $SU(4)$ quantum magnetism

Hui-Ke Jin^{*1}

¹TU Munich – Germany

Abstract

In this talk, I will discuss recent progress in combining fermionic Gaussian states with matrix product state. This method development not only enriches the tools for characterizing many fermionic parton ansatzes but also provides suitable initial states for improving the performance of the density matrix renormalization group method in two-dimensional systems. As an application, I will present our results on the $SU(4)$ spin-orbital antiferromagnetic Heisenberg model on a triangular lattice, for which we provide evidence that its ground state is a spinon Fermi surface consisting of open orbits in the reciprocal space. We also study the $SU(4)$ model on the honeycomb lattice and find that the ground states can be well described by a Gutzwiller projected π -flux state with Dirac-type gapless excitations.

^{*}Speaker

SU(N) symmetric Projected Entangled Pair States : construction and applications

Matthieu Mambrini*¹

¹Laboratoire de Physique Théorique – Université Paul Sabatier - Toulouse III, CNRS – France

Abstract

In the context of SU(N) two-dimensional SU(N) spin system, discrete (point group) and continuous symmetries can be implemented at a local (tensor) level in a PEPS (Projected Entangled Pair States) scheme. This construction makes it possible to design wavefunction manifolds with controlled broken/unbroken symmetries (1) while considerably reducing the number of free parameters.

This framework is not only useful for engineering particular states (such as chiral spin liquids (5,6,7)), but also for ground-state optimization procedures for a given Hamiltonian (2,3,4), for studying thermodynamic properties (8) or for investigating the real-time dynamics of 2d quantum systems (9,10,11).

In this talk, I will explain the main ideas of this construction and illustrate with some recent examples.

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*Speaker

Numerical methods to investigate SU(N) Fermi-Hubbard models.

Pierre Nataf^{*†1}

¹CNRS – LPMMC – France

Abstract

Systems of multicolor fermions have recently raised considerable interest due to the possibility to experimentally study those systems on optical lattices with ultracold atoms. To describe the Mott insulating phase of N-colors fermions, one can start with the SU(N) Fermi-Hubbard Model (FHM) (which encompass the standard Fermi-Hubbard model for electrons with spins 1/2 which corresponds to N = 2) . The theoretical description of such a model is however difficult due to the exponentially large dimension of the Hilbert space, scaling as 2^{NL} , where L is the number of sites. We found a way to perform exact diagonalizations (ED) of SU(N) FHM on L-sites clusters separately in each irreducible representation (irrep) of SU(N), which leads to a dramatic reduction of the dimension of the matrices to diagonalize. It is based on the representation theory of the unitary groups U(L), and is the proper generalization of the protocole developed for the Heisenberg SU(N) models, which was based on the representation theory of the symmetric group SL. This leads to a dramatic reduction of the dimension of the matrices to diagonalize. As an application of this color factorization, we study the robustness of some SU(N) phases predicted in the Heisenberg limit upon decreasing the on-site interaction on various lattices of size $L \leq 12$ and for $2 \leq N \leq 6$. In particular, we show that a long range color ordered phase emerges for intermediate U for N=4 at filling 1/4 on the triangular lattice. We finally present the numerical observation of the SU(N) Nagaoka's Ferromagnetism in the presence of one hole away from filling 1/N.

*Speaker

†Corresponding author: pierre.nataf@lpmmc.cnrs.fr

Theory and experiment on current noise of SU(N) Anderson impurity

Rui Sakano^{*†1}, Tokuro Hata², Kaiji Motoyama³, Akihiko Saeki³, Tomonori Arakawa⁴,
Meydi Ferrier⁵, Richard Deblock⁵, Teratani Yoshimichi³, Mikio Eto¹, Kensuke
Kobayashi⁶, and Akira Oguri³

¹Keio University – Japan

²Tokyo Institute of Technology [Tokyo] – Japan

³Osaka Metropolitan University – Japan

⁴The National Institute of Advanced Industrial Science and Technology – Japan

⁵Université Paris-Saclay – LPS Orsay – France

⁶University of Tokyo – Japan

Abstract

Development in experimental techniques has led to remarkable progress in investigating quantum many-body effects through artificially controlled quantum states in various physical systems. We will delve into recent theoretical and experimental developments regarding the SU(N) Kondo effect, manifested in quantum dots fabricated on semiconductor substrates with nanoscale.

The many-body low-energy state resulting from the Kondo effect is described by the local Fermi liquid theory, an extension of Landau's Fermi liquid. The values of the Fermi liquid parameters characterizing the system depend on the N of the SU(N) symmetry. The renormalized interaction gives rise to excited states, influencing nonlinear currents and current noise. Specifically, the renormalized interaction enhances current noise by generating charge-pair states within the current. Then the influence of the symmetry of the system can be seen in the measurement of the Fano factor. It is found that, beyond the previous understanding of the Fermi fluid theory, the correction introduced by the three-body correlation function significantly affects nonlinear current and current noise in SU(N) quantum dots (1, 2, 3). Using numerical renormalization group calculations, we elucidate this effect in quantum dots with SU(N) symmetry under the influence of a magnetic field to control the electronic state.

Carbon nanotube quantum dots have orbital states corresponding to the degrees of freedom of the motion of the electrons confined therein in the winding direction of the nanotube, in addition to the spin degrees of freedom. This allows the entire system to be described by the Anderson impurity model with SU(4) or SU(2) symmetry. We discuss the nonlinear current and current noise in carbon nanotube quantum dots by comparing theory with experimental observations (4).

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*Speaker

†Corresponding author: sakano@keio.jp

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- (3) Yoshimichi Teratani, Rui Sakano, and Akira Oguri, *Phys. Rev. Lett.* 125, 216801 (2020).
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Quantum Simulation Studies of the SU(3) Fermi-Hubbard Model

Richard Scalettar*¹

¹Department of Physics and Astronomy, University of California, Davis – United States

Abstract

We present the results of quantum Monte Carlo simulations and numerical linked cluster expansion calculations of the SU(3) symmetric Fermi-Hubbard model on a square lattice at 1/3-filling. Using an exact, finite temperature method, we first present the different regimes of the model in the T-U plane, which are characterized by local correlations, and capture signatures of the metal-insulator transition and magnetic crossovers. These signatures are detected as the temperature scales characterizing the rise of the compressibility, and an interaction-dependent change in the sign of the diagonal spin-spin correlation function. The analysis of the compressibility estimates the location of the metal-insulator quantum critical point at $U_c/t \sim 6$, and provides a temperature scale for observing Mott physics at finite T. Furthermore, from the analysis of the spin-spin correlation function we observe that for $U/t \sim 6$ and $T \sim J = 4t^2/U$, there is a development of a short-range two sublattice antiferromagnetic structure, as well as an emerging three sublattice antiferromagnetic structure as the temperature is lowered below $T/J \sim 0.57$. In order to examine the low temperature properties, we next employ a self-consistent variant of the constrained path quantum Monte Carlo approach. We find clear evidence of multiple, successive quantum critical points separating a non-magnetic uniform metallic phase at weak coupling from regimes with long range 'spin' order, whose symmetry changes as the interaction strength increases.

*Speaker

Towards encoding a qudit in the nuclear spin of 87-Sr

Florian Schreck*¹

¹University of Amsterdam [Amsterdam] = Universiteit van Amsterdam – Netherlands

Abstract

Qudits are generalizations of qubits to higher dimensional Hilbert spaces. They allow to store more quantum information in a single atom compared to qubits, potentially enabling more complex algorithms to be executed on quantum computers with a given number of atoms. 87-Sr has a nuclear spin of $I=9/2$ that is not coupled to the electronic structure in the atom's ground state, making it well suited to encode a qudit. As a first step towards this goal, I'll present a precision measurement of the 87-Sr nuclear g-factor made possible by using 87-Sr as co-magnetometer. Applying a tensor shift will allow to selectively drive rf transitions between neighboring m_I states. m_I state selective coupling to Rydberg states can allow 2-qudit gates.

*Speaker

Inter-valley coherence, intrinsic and extrinsic spin-orbit coupling in rhombohedral graphene

Owen Sheekey*¹

¹University of California, Santa Barbara – United States

Abstract

Rhombohedral graphene multilayers provide a clean and highly reproducible platform to explore the emergence of superconductivity and magnetism in a strongly interacting electron systems. The high density of states near the van Hove singularities lead to a variety of broken symmetry phases – including exotic forms of spin and valley ferromagnetism (2, 3). Because of their combined spin and valley ‘isospin’ degrees of freedom, these Stoner magnets exhibit an approximate $SU(4)$ symmetry with a near degeneracy in the many body phase diagram. In reality, this $SU(4)$ symmetry is only approximate, weak symmetry breaking arises even at the single particle level – in the form of intrinsic spin-orbit coupling. Here, we use high resolution thermodynamic compressibility measurements and nanoSQUID on tip (nSOT) magnetometry to study the effects that intrinsic spin-orbit coupling has on the magnetic phase diagram in rhombohedral graphene. By supporting rhombohedral graphene on a WSe2 substrate, ‘extrinsic’ strong spin-orbit coupling can be proximitized, significantly altering the phase diagram. We demonstrate the presence of an inter-valley coherent quarter metal which becomes strongly spin-valley locked when supported by WSe2. Our results shed light on the role proximity induced Ising spin-orbit coupling and intrinsic spin-orbit coupling plays in selecting the ground state in correlated graphene systems.

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(3) Arp, T., et. al. *arXiv:2310.03781* (2023).

*Speaker

Quantum simulation using ultracold Yb atoms with SU(N) symmetry

Yosuke Takasu*¹

¹Kyoto University – Japan

Abstract

Two-electron atoms such as Yb and Sr have been applied to quantum simulations due to the existence of narrow transitions (clock transitions) and fermionic isotopes with SU(N) degrees of nuclear spin freedom. Through the development of various observational techniques, our research group at Kyoto University has recently been studying quantum simulations of quantum many-body systems, for example, short-range spin correlations and dynamics under dissipation using fermionic Yb atoms with SU(N) symmetry in optical lattices. We are now developing new methods for measuring spin-correlation, such as a quantum gas microscope technique. In this talk, I will report the latest experimental results.

*Speaker

QSpace: An open-source tensor library for Abelian and non-Abelian symmetries

Andreas Weichselbaum^{*†}

¹Brookhaven National Laboratory – United States

Abstract

I will present the open-source tensor library QSpace built for tensor network states.

QSpace permits arbitrary combinations of symmetries including the Abelian symmetries Z_n and $U(1)$, as well as all non-Abelian symmetries based on the semi-simple classical Lie algebras A_n , B_n , C_n , and D_n , or respectively, the special unitary group $SU(n)$, the odd orthogonal group $SO(2n+1)$, the symplectic group $Sp(2n)$, and the even orthogonal group $SO(2n)$.

QSpace is designed as a bottom-up approach that starts from the defining representation and the Lie algebra. By explicitly computing and utilizing generalized Clebsch-Gordan coefficient tensors, this makes QSpace versatile in the type of operations that it can perform across all symmetries. At the level of an application, much of the symmetry-related details are hidden within the QSpace core libraries. Hence when developing tensor network algorithms with QSpace, these can be coded (nearly) as if there are no symmetries at all, despite being able to fully exploit general non-Abelian symmetries. This allows one to focus on the tensor algorithms of interest, irrespective of the symmetries used, as these are taken care of within QSpace.

^{*}Speaker

[†]Corresponding author: weichselbaum@bnl.gov

Fractional quantization of $SU(N)$ matter-wave persistent currents

Luigi Amico*¹

¹Quantum Research Centre, Technology Innovation Institute – United Arab Emirates

Abstract

Neutral atoms guided in ring-shaped atomtronic circuits present quantized values of the angular momentum per particle. Depending on the specific parameters characterizing the system (eg: nature of the particle statistics, interactions), the winding number present different quantization properties. In this talk, I will showcase how such a phenomenon occurs in an atomtronic circuit with a quantum fluid consisting of strongly interacting N -component fermions, the so-called $SU(N)$ fermions. For repulsive interactions a specific emerging phenomenon of attraction from repulsion appears, providing a quantization with similar properties to the attracting bosonic case. For attractive interactions, the quantization is determined by the number of components N . Schemes to read-out the persistent current fractionalization in cold atoms experiments will be provided.

*Speaker

Probe for bound states of SU(3) fermions and colour deconfinement

Wayne Jordan Chetcuti*^{†1}, Juan Polo¹, Andreas Osterloh¹, Paolo Castorina^{2,3}, and Luigi Amico^{1,2,4,5}

¹Quantum Research Center, Technology Innovation Institute, P.O. Box 9639 Abu Dhabi, UAE – United Arab Emirates

²INFN-Sezione di Catania, Via S. Sofia 64, 95127 Catania, Italy – Italy

³Institute of Particle and Nuclear Physics, Faculty of Mathematics and Physics, Charles University, Czech Republic – Czech Republic

⁴Dipartimento di Fisica e Astronomia, Via S. Sofia 64, 95127 Catania, Italy – Italy

⁵Centre for Quantum Technologies, National University of Singapore 117543, Singapore – Singapore

Abstract

In this talk, I will present our work on a mesoscopic ring-shaped potential comprised of strongly interacting SU(N) fermions pierced by an effective magnetic flux. By employing a combination of Bethe ansatz and numerical techniques (exact diagonalization and DMRG), we find that the formation of N -body bound states causes the angular momentum quantization per particle to acquire fractional values. Such a phenomenon manifests itself in the matter-wave flow of the system as a $1/N$ periodicity. Of particular interest in our analysis is the SU(3) case due to its relation with quantum chromodynamics (QCD). By taking trions and colour superfluid states (two types of SU(3) bound states) to be the analogues of hadrons and quark-quark pairs in QCD, we demonstrate that one can explore this crossover through persistent currents. Lastly, we consider finite temperature effects, where we find that an interplay between temperature and interaction can lead to a specific bound state deconfinement without explicitly breaking the SU(3) symmetry.

*Speaker

[†]Corresponding author: waynejordanc@gmail.com

Flow of an $SU(N)$ fermionic matter-wave through a localized barrier

Juan Polo Gomez^{*1}, Andreas Osterloh², Wayne Jordan Chetcuti², Anna Minguzzi³, and Luigi Amico²

¹Quantum Reserach Center, TII, UAE – United Arab Emirates

²Quantum Reserach Center, TII, UAE – United Arab Emirates

³Université Grenoble Alpes, CNRS, LPMMC, 38000 Grenoble, France – Grenoble Alpes University, CNRS, LPMMC, F-38000 Grenoble, France – France

Abstract

In this talk, I will present our recent investigations of matter-wave flow of $SU(N)$ fermions through a localized impurity in a mesoscopic ring pierced by an effective magnetic field.

In $SU(N)$ fermionic rings, the flow of particles can be controlled by the effective magnetic field, with a strong dependence on the interactions, which give rise to fractional values of the angular momentum. The underlying origin this phenomenon is due to the formation of composite bound states (attraction) and spinon excitations (repulsion).

I will explain how an impurity affects the persistent current in a complementary regime to the seminal work of Kane and Fisher, where we now focus on the mesoscopic regime. In bosonic systems, the barrier renormalizes the amplitude of the persistent current in a non-monotonous behavior, whereas for multi-component fermions, this has not been explored until now. Moreover, we observe that the smoothing out of the current, corresponding to a gap opening in the spectrum, only happens for particular states. We analyze the system through a combination of numerical and analytical approaches, including DMRG, Luttinger liquid theory, and Bethe ansatz, which allows us to understand the underlying reasons for the observed behavior.

^{*}Speaker

Symmetry Breaking Patterns in Itinerant $SU(N)$ Ferromagnetism

Chen-How Huang*¹

¹Donostia International Physics Center (DIPC) – Spain

Abstract

Ferromagnetic transitions in systems with $SU(N)$ symmetry are attracting much attention in recent years motivated by experiments on graphene multilayers and the possibility of realizing $SU(N > 2)$ symmetry in alkaline-earth ultracold atomic gases. Unlike $SU(2)$ systems where only one transition pattern between paramagnetic and ferromagnetic phases is possible, the enlarged unitary symmetry allows richer patterns of ferromagnetic transitions. In connection to this, it is interesting to note that graphene multilayer systems, where an approximate $SU(4)$ symmetry is realized when combining the electron spin and valley degrees of freedom, a cascade of phase ferromagnetic transitions has been experimentally observed. In this oral contribution, we will report results for the phase diagram and ferromagnetic phase transitions of interacting Fermi systems with $SU(N)$ symmetry with both short-range contact and long-range Coulomb interactions. Within Hartree-Fock approximation, we find a Fermi gas with short-range interactions undergoes a transition from the paramagnetic state to the fully polarized state. On the other hand, the paramagnetic state of the Fermi gas with long-range Coulomb interaction undergoes a cascade of $N - 1$ first-order phase transitions where one component is depopulated at a time until all electrons have identical $SU(N)$ spin. These two systems exhibit distinct ferromagnetic transition patterns at mean-field (Hartree-Fock) level. However, going beyond mean-field theory and accounting for the correlation energy within the random-phase approximation,

the cascade of phase transitions disappears and the transition pattern becomes the same as for the Fermi gas with short-range interactions. Nevertheless, we show that this resemblance is only superficial as the energy balance that drives the transition from the paramagnetic to the fully polarized state is dominated by different contributions to the total ground state energy.

In addition, we also report results for a different $SU(N)$ Fermi system on the Bethe lattice with short-range interactions in the mean field limit. In this system, an unconstrained minimization of the free energy obtained within Hartree-Fock yields a cascade of phase transitions as a function of the particle density and interaction strength, which shows that the phenomenology (i.e. cascade of transitions) observed in twisted bilayer graphene can be also realized in other models.

*Speaker

Ferromagnetic instability for the SU(N) Hubbard model

Juntaro Fujii¹ and Akihisa Koga^{*1}

¹Tokyo Institute of Technology – Japan

Abstract

Low-temperature properties in correlated fermion systems have attracted much attention since the discovery of the highTc cuprates. In the strongly correlated electron systems, the spin degrees of freedom play a crucial role in stabilizing interesting phenomena at low temperatures such as magnetism, superconductivity, and Mott phase transitions. The orbital degrees of freedom enrich the system. Recently, an optical lattice system, where the periodic potential is loaded into ultracold atoms, has been realized. In the system, various parameters can be controlled experimentally such as the hopping integrals, interaction strength, and lattice structure. Furthermore, spin and orbital degrees of freedom can be introduced, which makes strongly correlated fermion systems with multicomponents more interesting. One of the interesting and fundamental questions is how the symmetry-breaking state is realized in a multicomponent system. In our previous paper (1), we have considered the half-filled Hubbard model with repulsive interactions to clarify the instability for the antiferromagnetically ordered state. By contrast, the ferromagnetic instability in the SU(N) Hubbard model is less understood except for the SU(2) case. In the strong coupling limit in the SU(2) Hubbard model, itinerant nature of one hole on a lattice with a closed-loop structure leads to a fully polarized ferromagnetically ordered ground state, which is so-called Nagaoka ferromagnetism. Although similar results have been obtained in the SU(3) case (2), still controversial how this ordered state relates to the system with the finite hole density. What is the most important in this strong-coupling region is that large Coulomb interactions and low energy itinerant properties of electrons are necessary to deal with precisely in an equal footing.

In this study, we consider the multicomponent fermionic system, which is described by the SU(N) Hubbard model. We discuss how the ferromagnetically ordered state is realized at low temperatures, making use of dynamical mean-field theory with the continuous-time quantum Monte Carlo method.

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*Speaker

Dynamics of SU(3) spin coherent states: semiclassical method and its application to spin nematics and spin liquids in spin-1 magnets

Rico Pohle*¹

¹Tohoku University [Sendai] – Japan

Abstract

Spin-1 magnets allow for dipolar and quadrupolar moments on a single site, leading to rich physical properties as seen in spin nematic phases (1), Fe-based superconductors (2) and cold atom systems (3). However, experimental probing of these unconventional phases remains challenging, and therefore requires new theoretical tools to describe and interpret their ground state and excitation properties.

In this talk, we introduce a new Monte Carlo and Molecular Dynamics method designed for SU(3) spin coherent states, which can be used to study thermodynamic and dynamic properties of spin-1 magnets (4). We benchmark our numerical implementation by studying the ferroquadrupolar phase of the spin-1 bilinear-biquadratic (BBQ) Hamiltonian on the triangular lattice, and show excellent agreement with analytical flavour-wave theory and low-temperature expansion results.

Moreover, we demonstrate the advantage of this method through real-time dynamics simulations of topological vortices in a spin nematic (5) and unveiling a novel chiral spin liquid in the spin-1 Kitaev model with BBQ interactions (6).

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*Speaker

Three-body Fermi-liquid effects on transport through the $U=\infty$ $SU(N)$ Anderson impurity

Kaiji Motoyama^{*†1}, Kazuhiko Tsutsumi¹, Yoshimichi Teratani¹, Rui Sakano², and Akira Oguri¹

¹Osaka Metropolitan University – Japan

²Keio University [Tokyo] – Japan

Abstract

In this study, we explore how three-body Fermi-liquid corrections influence transport properties in an Anderson model with N degenerate energy levels. We consider the strong coupling limit where the interaction strength U approaches infinity and the impurity level occupancy, nd , varies between 0 and 1, which includes the Kondo regime and the valence fluctuation regime, depending on the impurity level ϵd . The three-body correlations among the impurity electrons emerge in the case where the system does not have the electron-hole or the time-reversal symmetries. Recent findings highlight the role of the three-body correlations which contribute to the low-energy behavior of transport coefficients, in addition to the other well-known Fermi-liquid parameters such as the phase shifts, the Wilson ratio, and the renormalization factors (1-3). Using the numerical renormalization group (NRG) method, we calculate these next-leading order terms of nonlinear conductance, current noise, and thermal conductance of $SU(N)$ quantum dots for $N=4$. In this presentation, we also discuss the implications of three-body effects on transport phenomena. (1) A. Oguri, and A. C. Hewson, PRL 120, 126802 (2018). (2) M. Filippone, C. Moca, A. Weichselbaum, J. von Delft, and C. Mora, PRB 98, 075404 (2018). (3) C. Mora, P. Vitushinsky, X. Leyronas, A. A. Clerk, and K. Le Hur, PRB 80, 155322 (2009). *K.M. was supported by JST Establishment of University Fellowships towards the Creation of Science Technology Innovation Grant No. JPMJFS2138.

*Speaker

†Corresponding author: sw23976y@st.omu.ac.jp

Interaction effects on the itinerant ferromagnetism phase transition

Jordi Pera^{*1}, Joaquim Casulleras^{*1}, and Jordi Boronat^{*1}

¹Universitat Politècnica de Catalunya – Spain

Abstract

We present a thorough study of the transition nature of Fermi gases. The exploration can be done thanks to the use of a third order perturbation formula for the energy system. At this level, there are three scattering parameters in play, those are, the S-wave scattering length a_0 , the S-wave effective range r_0 and the P-wave scattering length a_1 . We show that the spin value is not determinant in saying the nature of the phase transition. For any spin value, any kind of phase transition can happen depending on the potential. We show how the different transitions are encountered as a function of r_0 and a_1 , which are in units of a_0 , for $S=1/2$ up to $S=9/2$. Moreover, we then present a model based on Landau theory in order to proof this rich variability.

*Speaker

Interpretable phase classification on trapped ion experiment data by tensorial-kernel SVM

Nicolas Sadoune^{*†1} and Lode Pollet

¹Fakultät für Physik - Ludwig-Maximilians-Universität [München/Munich] – Germany

Abstract

Experimental progress in qubit manufacturing calls for the development of new theoretical tools to analyze quantum data. We show how an unsupervised machine-learning technique can be used to understand $SU(N)$ models using data of local measurements from trapped-ion experiments. We demonstrate the method by constructing the phase diagram of a $SU(2)$ and $SU(3)$ model and show that it detects the respective order parameters of its phases, including string order parameters. Prior information of the underlying Hamiltonian or the quantum states is not needed; instead, the machine outputs their characteristic observables. Our work opens the door for a first-principles application of hybrid algorithms that aim at strong interpretability without supervision.

*Speaker

†Corresponding author: nicolas.sadoune@physik.uni-muenchen.de